Birla Institute of Technology & Science, Pilani Mid Semester Test (Closed Book), First Semester 2022 – 2023 General Mathematics I (BITS F113)

Date: 02nd January, 2023 Max. Time: 90 Minutes Max. Marks: 30

Note. Answer all questions. Start answering each question on a fresh page.

- 1. How many words, with or without meaning can be made from the letters of the word **MONDAY**, assuming that no letter is repeated, if
 - (a) all letters are used at a time but first letter is a consonant, [1.5]
 - (b) all letters are used but the vowels come together? [1.5]
- 2. Show that $9^{n+1} 8n 9$ is divisible by 64, whenever n is a positive integer. [4]
- 3. If A.M. and G.M. of roots of a quadratic equation are 8 and 5, respectively, then find the roots. Hence, obtain the quadratic equation. [4]
- 4. If the slope of a line is double of the slope of another line and tangent of the angle between them is $\frac{1}{3}$, find the slopes of the lines. [4]
- 5. Find the coordinates of the focus, axis of the parabola, the equation of the directrix and the length of the latus rectum of the parabola $x^2 = -9y$. [4]
- 6. Find the equation of the line which pass through origin and lies on the plane through the intersection of the planes 3x-y+2z-4=0 and x+y+z-2=0. [4]
- 7. Suppose $f = \begin{cases} a + bx & x < 1 \\ 4 & x = 1, \text{ and if } \lim_{x \to 1} f(x) \text{ exists, what are possible values of } a \\ b ax & x > 1 \end{cases}$

and b? what are the possible values of a and b so that f is continuous at x = 1. [4]

8. Find the derivative of the function $\frac{4x + 5\sin x}{3e^x + 7\cos x}$ at x = 0. [3]