

**BIRLA INSTITUTE OF TECHNOLOGY AND SCIENCE, PILANI**  
**Second Semester 2017-2018**  
**Comprehensive Examination**

**CHE F342: Process Dynamics and Control**

**Date:** 1<sup>st</sup> May 2018

**Time:** 8.00 – 11.00 A.M.

**Maximum Marks:** 120

1. **(15 Marks)** The set point of the control system shown in Fig Q1 is given a step change of 0.1 unit.

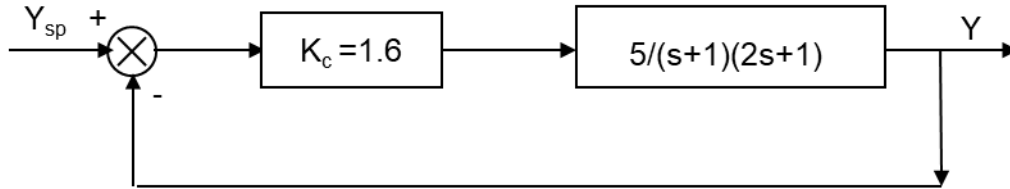


Fig Q1

Determine

- (a) The maximum value of Y and the time at which it occurs
  - (b) The offset
  - (c) The period of oscillation
2. **(15 Marks)** (a) What is BIBO stability criterion? Define stability for linear transfer function models and state-space models?  
 (b) The state-space model of the system is given by

$$\frac{dx_1}{dt} + 3x_1 - x_2 - u_1 + 2u_2 = 0$$

$$\frac{dx_2}{dt} - 2x_1 + 3x_2 - 2x_3 - 2u_2 = 0$$

$$\frac{dx_3}{dt} - x_2 + 3x_3 + 5u_3 = 0$$

Determine the stability of this system.

- (c) Using Routh Test determine the value of  $K_c$  for which the system shown in Fig Q2 will be stable.

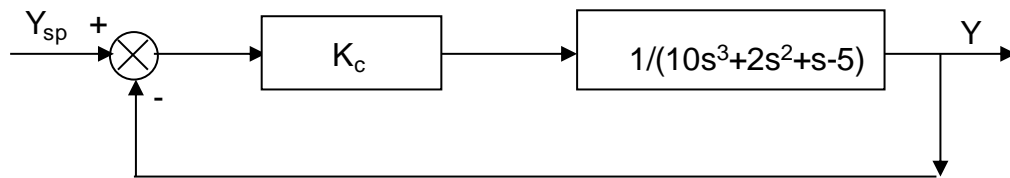


Fig Q2

3. **(30 Marks)** (a) What is Bode stability criterion? Explain gain margin (GM) and phase margin (PM) with a neat diagram.

(b) In the control system shown in Fig Q3 the transfer functions are  $G_c = K_c$ ,  $G_v = 1/(10s+1)$ ,  $G_p = 1/(s+1)$ ,  $G_{m1} = e^{-\theta s}$ ,  $G_{m2} = 1/(s+1)$ . The gain  $K_c$  is increased until the system oscillates continuously at a frequency of 3 rad/min. Calculate the value of time delay  $\theta$ .

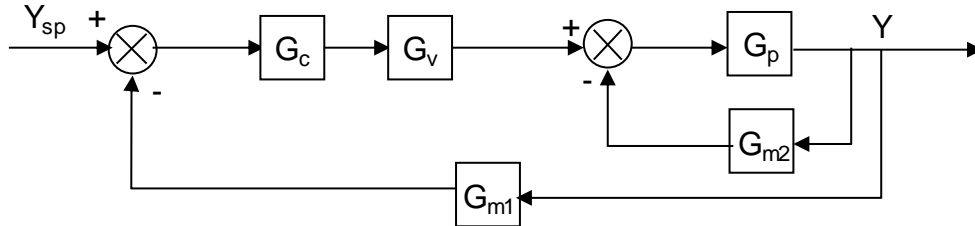


Fig. Q3

(c) For a system with  $G_c = K_c[1+(1/2s)]$ ,  $G_v = 1$ ,  $G_p = 1/(s+1)^2$ ,  $G_m = 1$ , determine the value of  $K_c$  for a Phase Margin of  $30^\circ$ . What is the Gain Margin in this case?

(d) Obtain the Z-N settings of a PID controller for a system with  $G_p = e^{-1.02s}/(s+1)$ ,  $G_v=G_m=1$ ,  $G_d=3/(5s+1)$  using Bode method and Direct Substitution (DS) method. Use Taylor approximation for time delay term in case of DS method.

4. (15 Marks) (a) Explain the terms: Bias, Proportional Band, reset time, offset.  
 (b) A closed-loop system has following transfer functions:

$$G_c = 3, G_v = 1, G_p = \frac{10}{(8s^2 + 24s + 2)}, G_m = 1.$$

Obtain the closed-loop response of the system for a unit step change in the set point. What is its value at  $t = 4$  time units and what is the offset?

5. (15 Marks) (a) Explain the time integral criteria and simple performance criteria for controller tuning. (b) Find the gain of a proportional controller that produces a closed loop response for a second order system with decay ratio equal to  $1/4$ . The process is described by

$$G_p = \frac{1}{s^2 + 3s + 1}, G_v = 1, G_m = 1.$$

6. (15 Marks) (a) Define the terms: sensor, transmitter, transducer.  
 (b) Write the equation to specify the size of a valve in terms of its capacity. Draw valve characteristics and show their equations.

7. (15 Marks) A liquid storage tank has two inlet streams with mass flow rates  $w_1$  and  $w_2$  and an exit stream with flow rate  $w_3$ .  $w_3$  is established by a valve on the outflow line according to  $w_3 = Cv h$  where  $h$  is the liquid level in the tank and  $Cv$  is the valve constant. The tank is 2.5 m tall and 2m in diameter. The steady state values are  $w_1 = 120$  kg/min,  $w_2 = 100$  kg/min and  $h = 1.75$ m.

- (i) What is the steady state value of  $w_3$  and value of valve constant  $Cv$ ?  
 (ii) If  $w_1$  is changed from 120 kg/min to 100 kg/min, what will be the final value of the tank level?