

SOLUTION

BIRLA INSTITUTE OF TECHNOLOGY & SCIENCE PILANI

SECOND SEMESTER 2022-2023

CHE F342: Process Dynamics & Control

Mid-Term Test

Date: 18.03. 2023

Duration: 2:00 - 3:30 PM

Max. Marks: 90 Min

Name:	Roll No:
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Section-I: PART A (Close Book) : Answer the questions in the space provided 10 x 2 = 20 M

1. The system has a transfer function $G(s) = \frac{3e^{-3s}}{(s+3)}$. When a step change of magnitude is M is given to the system input, the final value of the output is measured to be 40. The value of M is

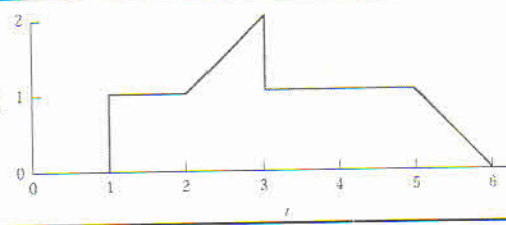
40

2. Two 1st order tanks are connected in a non-interacting manner. For a given step change in inlet flow rate, the nature of the response of the 2nd tank height is_ ($A_1 = A_2 = 1 \text{ m}^2$, $R_1 = R_2 = 1 \text{ sec/m}^2$, linear)

Non oscillatory / Stable response

3. The Laplace transform $f(s)$ for the following $f(t)$


$$\frac{e^{-s} - e^{-3s}}{s} + \frac{e^{-2s} - 6e^{-3s} - 3e^{-5s}}{s^2}$$



4. Plot $f(t)$, if a forcing function $f(t)$ has the Laplace transform $f(s) = \frac{1 - 2e^{-s} + e^{-2s}}{s^2}$.

$$t \cdot u(t) - 2(t-1)u(t-1) + (t-2)u(t-2)$$

$f(t)$



5. $\frac{dx}{dt} = \int_0^t x(t) dt - t$; $x(0) = 3$, then $x(t)$ is

$$x(t) = 1 + e^{-t} + e^t$$

6. A process of unknown transfer function is subjected to a unit-impulse input. The output of the process is measured accurately and is found to be represented by the function $y(t) = te^{-t}$. Determine the unit-step response of this process.

$$1 - e^{-t} - te^{-t}$$

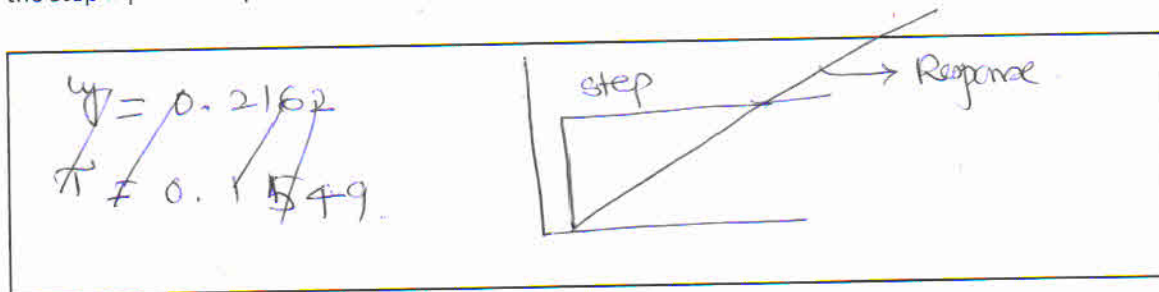
7. A unit gain 2nd order underdamped process has a period of oscillation 1.0 second and a decay ratio 0.25. The transfer function of the process is _

$$P.O = \frac{2\pi T}{\sqrt{1-\zeta^2}} \quad \zeta = 0.1549$$

$$D.R = \exp\left(\frac{-2\pi\zeta}{\sqrt{1-\zeta^2}}\right) \quad \zeta = 0.2162$$

$$\frac{1}{(0.1549s)^2 + 2(0.2162)(0.1549)s + 1}$$

8. A unit step change is given to a pure capacitance system. Draw the nature of the response and indicate the step input in the plot.



9. If $G(s) = \frac{1}{s+1} - \frac{2}{s+4}$, upon a unit step change in disturbance at $t = 0$, then the slope at $t = 0^+$ (just after the step change) is _____ & is the response stable?

Slope is negative & Inverse response.

10. Compare the responses of a second order system with $\xi = 0.01, 0.1, 1$ & 2 for a given unit step change in load variable. (indicate the ξ values on the responses)

