# CHEM F111 GENERAL CHEMISTRY <br> Mid-Semester Examination (Closed Book) <br> Duration: 90 minutes 

Max. Marks: 90
Date: $07^{7 \text { th }}$ October 2016
NOTE: There are FIVE questions in all. Attempt all the questions. Start answering each question on a fresh page and answer all parts of the question together. Pencil should not be used. Symbols have usual meanings. Do not scribble on the question paper.

USEFUL DATA: $\sigma=5.6697 \times 10^{-8} \mathrm{Wm}^{-2} \mathrm{~K}^{-4} ; \mathrm{b}=2.9 \mathrm{mmK} ; \mathrm{c}=3 \times 10^{8} \mathrm{~m} / \mathrm{s}$; Mass of electron $=9.109 \times 10^{-31} \mathrm{~kg}$
$1 \mathrm{amu}=1.66 \times 10^{-27} \mathrm{~kg} ; a_{0}=0.529 \AA ; \mathrm{h}=6.626 \times 10^{-34} \mathrm{Js} ; \mathrm{R}=8.314 \mathrm{JK}^{-1} \mathrm{~mol}^{-1} ; 1 \mathrm{bar}=101.3 \mathrm{kPa}$
Standard integral: $\int \sin ^{2} b x d x=\frac{x}{2}-\frac{1}{4 b} \sin 2 b x ; 1 \AA=10^{-10} \mathrm{~m} ; 1 \mathrm{~nm}=10^{-9} \mathrm{~m}$
Q. 01. (a) An average human body has a surface area of $0.1 \mathrm{~m}^{2}$. Assuming human body behaves like a black body, calculate power emitted by this body at $37^{\circ} \mathrm{C}$ ?
(b) A linear conjugated molecule of length, $L$, can be approximated using the particle in a one-dimensional box. The wavefunction corresponding to one of the energy levels is given by $\psi=\sqrt{\frac{2}{L}} \sin \frac{3 \pi x}{L} ; \quad 0 \leq x \leq L$
(i) Write the number of node(s), if any, present in the energy level corresponding to the given wavefunction.
(ii) Evaluate probability of finding the electron described by the above wavefunction within 0.4 L to 0.5 L .
(iii) If the length, $L$, of the molecule is $12 \AA$, calculate the wavelength (in $\mathbf{n m}$ ) of the electromagnetic radiation required to excite the electron from $n=5$ to $n=6$ level.
[1+4+4]
(c) A particle of mass, $M$, moving in a two-dimensional ring of radius, $r$, is associated with zero potential energy and is represented by a wavefunction $\psi_{m}(\phi)=e^{i m \phi}$; where $m$ is rotational quantum number:
(i) Write down the expression of Hamiltonian operator (in polar coordinates).
(ii) Determine the magnitude of kinetic energy associated with this particle when it is present in the ground energy level; given that the moment of inertia, $I$, is $4 \times 10^{-42} \mathrm{~kg} \mathrm{~m}^{2}$.
(iii) Normalize the wavefunction, $\psi_{m}(\phi)$, and determine the value of normalization constant.
Q. 02. (a) The expression of a particular orbital of a hydrogenic atom $\left(B^{x+}\right)$ is,
$\psi=\frac{1}{4(2 \pi)^{1 / 2}}\left(\frac{3}{a_{0}}\right)^{3 / 2}\left(\frac{3 r}{a_{0}}\right) e^{-3 r / 2 a_{0}} \cos \theta$
(i) Fill up the following table on the basis of the above information (Answer the question in the tabular format by drawing table in your answersheet as given below):

| Atomic Symbol $(B)$ | Atomic charge $(x)$ | $n$ | $l$ | $\left\|m_{l}\right\|$ |
| :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |

(ii) Write the expressions for Coulomb potential energy and total energy corresponding to this orbital.
(iii) Determine the numbers of radial and angular node(s), if any, present in this orbital.
(b) Determine the electronic configuration for an atom belonging to $2^{\text {nd }}$ period of the periodic table with the ground state term symbol ${ }^{4} \mathrm{~S}_{3 / 2}$.
(c) Calculate the most probable radius at which an electron will be found when it occupies 1s orbital with radial distribution function, $P(r)=\frac{4 Z^{3}}{a_{0}^{3}} r^{2} e^{-2 Z r / a_{0}}$ of a hydrogenic atom, $\mathrm{O}^{7+}$ in Angstrom unit $(\AA)$ ).
Q. 03. (a) Calculate the spacing between the $3^{\text {rd }}$ and $6^{\text {th }}$ spectral lines $\left(i n \mathrm{~cm}^{-1}\right.$ ) in the rotational spectrum of ${ }^{1} \mathrm{H}^{35} \mathrm{Cl}$ molecule having bond length of 0.127 nm .
(b) IR spectra of two pairs of compounds: (i) $\left[\mathrm{CH}_{3} \mathrm{C} \equiv \mathrm{N}\right.$ and $\left.\mathrm{CH}_{3} \mathrm{C} \equiv \mathrm{CCH}_{3}\right]$, and (ii) $\left[\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CH}_{2} \mathrm{NH}_{2}\right.$ and $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CH}_{2} \mathrm{CONH}_{2}$ ] are given to you. Write the distinguishable IR band(s) for each given pair of compounds.
(c) The force constant for HF molecule is $9.7 \times 10^{2} \mathrm{~N} \mathrm{~m}^{-1}$. Calculate the wavenumber (in $\mathrm{cm}^{-1}$ ) of IR radiation to excite the molecule from $\boldsymbol{n}=\mathbf{0}$ to $\boldsymbol{n}=\mathbf{1}$, where $n$ is the vibrational quantum number.
(d) Arrange the following compounds (I, II and III), in order of decreasing $\bar{v}_{\mathrm{C}=\mathrm{O}}$ stretching frequency. Give reasons for the order chosen. Explanation for each compound is required.

Q. 04. (a) A compound $\mathrm{C}_{8} \mathrm{H}_{18} \mathrm{O}_{2}$ with a strong broad IR absorption band at $3293 \mathrm{~cm}^{-1}$ exhibits peaks at $\delta 1.22(12 \mathrm{H}$, singlet), $1.57\left(4 \mathrm{H}\right.$, singlet) and $1.96\left(2 \mathrm{H}\right.$, broad singlet) in ${ }^{1} \mathrm{H}-\mathrm{NMR}$ spectrum. The proton decoupled ${ }^{13} \mathrm{C}$ NMR of this compound consists of three lines resonating at $\delta 29.4,37.8$ and 70.5 . Identify the structure of compound and assign given chemical shift values of ${ }^{\mathbf{1}} \mathbf{H}$-NMR for different group of protons.
(b) A NMR signal is appearing 120 Hz downfield from TMS in an instrument operating at 300 MHz . (i) What is signal's chemical shift ( $\delta$ )? (ii) What would be its chemical shift if the spectra is recorded in an instrument operating at 100 MHz ?
(c) Complete the following table by writing all the information for compound [A] in given format at one place.
(Answer the question in the tabular format by drawing table in your answersheet as given below) [1+2+1+2]

| Compound [A] | Number of peaks <br> in ${ }^{1} \mathrm{H}$ NMR | Label the most <br> de-shielded protons | Multiplicity of <br> each peak in ${ }^{1} \mathrm{H}$ <br> NMR | Number of peaks in <br> proton decoupled ${ }^{13} \mathrm{C}$ <br> NMR |
| :---: | :--- | :--- | :--- | :--- |
| $\mathrm{CH}_{3} \mathrm{OCH}_{2} \mathrm{OCH}_{2} \mathrm{CH}_{3}$ |  |  |  |  |

Q. 05. (a) Reduction of $\mathrm{Fe}(\mathrm{III})$ oxide by carbon is presented as, $2 \mathrm{Fe}_{2} \mathrm{O}_{3}(s)+3 \mathrm{C}(s) \longrightarrow 4 \mathrm{Fe}(s)+3 \mathrm{CO}_{2}(\mathrm{~g})$; Using the data provided in the table given below, determine: (i) $\Delta_{\mathrm{r}} \mathrm{H}^{\varnothing}{ }_{298}$, (ii) $\Delta_{\mathrm{r}} \mathrm{S}^{\varnothing}{ }_{298}$, (iii) $\Delta_{\mathrm{r}} \mathrm{G}^{\varnothing}{ }_{298}$, and (iv) estimate the minimum temperature at which the reaction becomes spontaneous at 1 bar pressure.
$[2+2+2+2]$

|  | $\mathbf{F e}_{2} \mathbf{O}_{\mathbf{3}}(\mathbf{s})$ | $\mathbf{C}(\mathbf{s})$ | $\mathbf{F e}(\mathbf{s})$ | $\mathbf{C O}_{2}(\mathbf{g})$ |
| :--- | :--- | :--- | :--- | :--- |
| $\mathbf{\Delta}_{\mathbf{f}} \mathbf{H}^{\varnothing}{ }_{298}\left(\mathbf{k J m o l}^{\mathbf{- 1}}\right)$ | -824.2 | 0 | 0 | -393.5 |
| $\mathbf{S}^{\varnothing}{ }_{298}\left(\mathbf{J K}^{-1} \mathbf{m o l}^{-\mathbf{1}}\right)$ | 87.4 | 5.7 | 27.3 | 213.7 |

(b) The normal boiling point of a solvent is $80^{\circ} \mathrm{C}$ and its $\Delta_{\text {vap }} \mathrm{H}=30.8 \mathrm{kJmol}^{-1}$. Assuming that $\Delta_{\text {vap }} \mathrm{H}$ is independent of temperature in the temperature range and that the vapor behaves ideally, calculate its boiling point at 5 kPa .
(c) The mechanism of $\mathrm{Br}^{-}$-catalyzed aqueous reaction, $\mathrm{H}^{+}+\mathrm{HNO}_{2}+\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{NH}_{2} \xrightarrow{\mathrm{Br}^{-}} \mathrm{C}_{6} \mathrm{H}_{5} \mathrm{~N}_{2}^{+}+2 \mathrm{H}_{2} \mathrm{O}$, is described below,

Step 1: $\mathrm{H}^{+}+\mathrm{HNO}_{2} \xrightarrow{k_{1}} \mathrm{HNO}_{2}^{+}$
Step $2: \mathrm{HNO}_{2}^{+} \xrightarrow{k_{-1}} \mathrm{H}^{+}+\mathrm{HNO}_{2}$
(i) Identify the reaction intermediates, $I_{1}$ and $I_{2}$;
(iii) Determine: $\frac{d}{d t}\left[I_{1}\right]$ and $\frac{d}{d t}\left[I_{2}\right]$;
(iv) Determine the expression of $\boldsymbol{r}$ using Steady State Approx.
$[1+1+2+3]$

