# Birla Institute of Technology \& Science, Pilani, Rajasthan - 333031 

First Semester 2022-2023, Mid Semester Examination (Open Book)

Subject: Physical Chemistry -I (PC-1)<br>Course Code: CHEM F211

Duration: 90 minutes
Date: November 4, 2022
Max. Marks: 60
Note: Please check that the question paper is printed on both sides. Attempt all the questions. Start answering each question on a fresh page and answer all parts of the question together. Pencil should not be used. Symbols have usual meaning.

Do not scribble on the question paper.
Q1. (i) At 573 K temperature and 0.60 atm. pressure the Joule-Thomson coefficient of $\mathrm{N}_{2}$ is given by $\mu=0.0142-2.60 \times 10^{-4} P$. Assuming the equation to be independent of temperature near $300^{\circ} \mathrm{C}$ determine the temperature drop which may be expected on Joule-Thompson expansion of the gas from 60 atm. to 20 atm.
[3 M]
(ii) For an ideal gas, $\left(\frac{\partial U}{\partial V}\right)_{T}=0$, from this information show that $\left(\frac{\partial C_{V}}{\partial V}\right)_{T}=0$. Here, $U$ and $C_{V}$ are the internal energy and specific heat at constant volume respectively.
(iii) Establish the relation $C_{P}-C_{V}=\frac{\alpha^{2} V T}{\beta}$, where $\alpha$ and $\beta$ is the thermal expansivity and isothermal compressibility respectively. $C_{p}$ and $C_{V}$ is the specific heat at constant pressure and constant volume respectively. T is the temperature and V is the volume.
[5 M]
(iv) Define Helmholtz free energy ( A ) and explain its physical significance in just one sentence. Calculate $\Delta \mathrm{A}$ for the vaporization of 0.1 mole $\mathrm{H}_{2} \mathrm{O}$ at 1.0 atm . pressure and $100^{\circ} \mathrm{C}$. [Given, molar volume of $\mathrm{H}_{2} \mathrm{O}(\mathrm{I})$ at $100^{\circ} \mathrm{C}$ is $18.8 \mathrm{ml} \mathrm{mol}^{-1}$ and that of $\mathrm{H}_{2} \mathrm{O}(\mathrm{g})$ is $30.6 \mathrm{~L} \mathrm{~mol}^{-1}$.
(v) One mole of an ideal monoatomic gas undergoes a reversible isothermal change at $25^{\circ} \mathrm{C}$ temperature and 1 atm pressure. The final volume of the gas after the change is twice its initial volume. Calculate heat $(q)$, work done $(w)$ and enthalpy change $(\Delta H)$ for this process.

Q2. (i) Compare the thermodynamic efficiency of the following engines. (a) An engine operates between 1000 K and 300 K , and (b) a combination of two engines where the first engine operates between 1000 K and 600 K and waste heat is passed to the second engine working between 600 K and 300 K .
(ii) A given mass of an ideal gas ( $C_{P}=5$ Cal K $K^{-1}$ mole ${ }^{-1}$ ) at $27^{\circ} \mathrm{C}$ is compressed adiabatically and reversibly to one quarter of its volume. Calculate the temperature after compression. Here $C_{p}$ is the specific heat at constant pressure.
(iii) The coefficient of compressibility ( $\beta$ ) of water at 298 K is $4.9 \times 10^{-6} \mathrm{~atm}^{-1}$, over the pressure range 1 to 25 atm. Calculate the amount of work required to compress a 1 mole liquid water from 1 atm. to 25 atm. at 298 K temperature. Compare this work with work involved in the compression of 1 mole ideal gas from 1 atm. to 25 atm. at 298 K temperature. In both cases consider the process as reversible. Please provide the unit in Joules. (Density of water is $\mathbf{1 g m} / \mathbf{m l}$ at $\mathbf{2 9 8} \mathrm{K}$ )
(iv) One mole of an ideal gas with $C_{V}=3.0 \mathrm{cal}^{-1} \mathrm{~mol}^{-1}$ initially at 273 K temperature, 1 atm . pressure and 22.4 litre volume is put through the following reversible cycle:
(a) State 1 to state 2, heated at constant volume to twice the initial temperature.
(b) State 2 to state 3 expanded adiabatically until it is back to initial temperature.
(c) State 3 to state 1 compressed isothermally back to state 1.

Depict the cycle in V vs T diagram and calculate the amount of heat transfer (q), work (w) and change in internal energy $(\Delta U)$ for this cycle. Write in just one sentence what conclusion you can derive from the results.
[5 M]
Q3. (i) Calculate the enthalpy change $(\Delta \mathrm{H})$ at 1500 K for the reaction $2 \mathrm{H}_{2}(g)+\mathrm{O}_{2}(g) \rightleftharpoons$ $2 \mathrm{H}_{2} \mathrm{O}(\mathrm{g})$, given that, $\Delta \mathrm{H}_{300 \mathrm{~K}}=115.0 \mathrm{Kcal}$ and the values of $\mathrm{C}_{\mathrm{P}}\left(\mathrm{cal} \mathrm{mol}^{-1} \mathrm{~K}^{-1}\right)$ are for $\mathrm{H}_{2}(\mathrm{~g})=6.95$ $-0.0002 \mathrm{~T}, \mathrm{O}_{2}(\mathrm{~g})=6.10+0.0032 \mathrm{~T}$ and $\mathrm{H}_{2} \mathrm{O}(\mathrm{g})=7.19+0.0024 \mathrm{~T}$. Here $\mathrm{C}_{\mathrm{P}}$ is the specific heat at constant pressure.
(ii) Calculate the change in entropy, $\Delta \mathrm{S}$, when 10 gm of ice at $0^{\circ} \mathrm{C}$ is added to 50 gm of water at $40^{\circ} \mathrm{C}$ in an isolated system. The latent heat of fusion of ice is $79.7 \mathrm{cal} \mathrm{gm}^{-1}$, the specific heat of water is $1 \mathrm{cal} \mathrm{gm}^{-1} \mathrm{~K}^{-1}$.
(iii) What is the boiling point of water at a place where the atmospheric pressure is 600 mm Hg ? The latent heat of vaporization is $540 \mathrm{cal} / \mathrm{gm}$.
[3 M]
(iv) Calculate the change in Gibbs free energy $(\Delta G)$ when 36 gm of water initially at $100^{\circ} \mathrm{C}$ and 10 atm. pressure are converted to vapor at $100^{\circ} \mathrm{C}$ and 0.01 atm . pressure. Given density of water is $1 \mathrm{gm} / \mathrm{ml}$ and the vapor obeys ideal gas law.

Q4. (i) Calculate the number of phases (P), components $(C)$ and degrees of freedom $(F)$ of the following systems at equilibrium.
(a) An aqueous solution of $\mathrm{H}_{2} \mathrm{SO}_{4}$ and $\mathrm{CH}_{3} \mathrm{COOH}$
(b) Water at its freezing point.
(c) A saturated solution of $\mathrm{Na}_{3} \mathrm{PO}_{4}$ which is completely dissociates into its component ions, contains an excess of salt.
(ii) At $140^{\circ} \mathrm{C}$, the vapor pressure of pure $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{Cl}$ is 939.4 mm of Hg and that of pure $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{Br}$ is 495.8 mm of Hg . If a liquid mixture of $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{Cl}$ and $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{Br}$ forms an ideal solution, what will be the composition of the mixture in the liquid phase, which boils at $140^{\circ} \mathrm{C}$ under 1 atm. pressure? What will be composition in the vapor phase at this temperature?
(iii) The following standard enthalpies of formation ( $\Delta H_{f}^{0}$ ) and entropies ( $S^{0}$ ) of the substances at $25^{\circ} \mathrm{C}$ are given

| Substance | $\Delta \boldsymbol{H}_{\boldsymbol{f}}^{\mathbf{0}}(\mathbf{K c a l})$ | $\boldsymbol{S}^{\mathbf{0}}\left(\boldsymbol{C a l ~ K}^{\mathbf{- 1}}\right)$ |
| :---: | :---: | :---: |
| Methane $\left(\mathrm{CH}_{4}, \mathrm{~g}\right)$ | -17.89 | 44.5 |
| Formaldehyde $(\mathrm{HCHO}, \mathrm{g})$ | -27.7 | 52.3 |
| Ethyl alcohol $\left(\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}, \mathrm{I}\right)$ | -66.4 | 38.4 |

Calculate the standard free energy change and equilibrium constant at $25^{\circ} \mathrm{C}$ and 1 atm. pressure for the reaction $\mathrm{CH}_{4}(g)+\mathrm{HCHO}(g) \rightleftharpoons \mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}(l)$.
[4 M]
(iv) Calculate activity coefficient of $\mathrm{Ba}^{2+}$ and $\mathrm{Cl}^{-}$in a 0.05 M aqueous solution of $\mathrm{BaCl}_{2}$ at $25^{\circ} \mathrm{C}$. Also determine the mean activity coefficient of $\mathrm{BaCl}_{2}$ in this solution at $25^{\circ} \mathrm{C}$. The Debye-Huckel constant, $\mathrm{A}=0.509$ for an aqueous solution at $25^{\circ} \mathrm{C}$.
[3 M]

