## Birla Institute of Technology & Science, Pilani, Rajasthan – 333031

First Semester 2022-2023, Mid Semester Examination (Open Book)

Subject: Physical Chemistry -I (PC-1)

Course Code: CHEM F211

Duration: 90 minutesDate: November 4, 2022Max. Marks: 60

**Note**: Please check that the question paper is printed on both sides. Attempt all the questions. **Start answering each question on a fresh page and answer all parts of the question together**. Pencil should not be used. Symbols have usual meaning.

## Do not scribble on the question paper.

**Q1**. (i) At 573 K temperature and 0.60 atm. pressure the Joule-Thomson coefficient of N<sub>2</sub> is given by  $\mu = 0.0142 - 2.60 \times 10^{-4} P$ . Assuming the equation to be independent of temperature near 300<sup>o</sup>C determine the temperature drop which may be expected on Joule-Thompson expansion of the gas from 60 atm. to 20 atm. [3 M]

(ii) For an ideal gas,  $\left(\frac{\partial U}{\partial V}\right)_T = 0$ , from this information show that  $\left(\frac{\partial C_V}{\partial V}\right)_T = 0$ . Here, U and C<sub>V</sub> are the internal energy and specific heat at constant volume respectively. [2 M]

(iii) Establish the relation  $C_P - C_V = \frac{\alpha^2 VT}{\beta}$ , where  $\alpha$  and  $\beta$  is the thermal expansivity and isothermal compressibility respectively.  $C_P$  and  $C_V$  is the specific heat at constant pressure and constant volume respectively. T is the temperature and V is the volume. [5 M]

(iv) Define Helmholtz free energy (A) and explain its physical significance in just one sentence. Calculate  $\Delta A$  for the vaporization of 0.1 mole H<sub>2</sub>O at 1.0 atm. pressure and 100°C. [Given, molar volume of H<sub>2</sub>O(I) at 100°C is 18.8 ml mol<sup>-1</sup> and that of H<sub>2</sub>O(g) is 30.6 L mol<sup>-1</sup>. [3 M]

(v) One mole of an ideal monoatomic gas undergoes a reversible isothermal change at  $25^{\circ}$ C temperature and 1 atm pressure. The final volume of the gas after the change is twice its initial volume. Calculate heat (q), work done (w) and enthalpy change ( $\Delta$ H) for this process. [2 M]

Q2. (i) Compare the thermodynamic efficiency of the following engines. (a) An engine operates between 1000 K and 300 K, and (b) a combination of two engines where the first engine operates between 1000 K and 600 K and waste heat is passed to the second engine working between 600 K and 300 K. [4 M]

(ii) A given mass of an ideal gas ( $C_P = 5 \ Cal \ K^{-1} \ mole^{-1}$ ) at 27<sup>o</sup>C is compressed adiabatically and reversibly to one quarter of its volume. Calculate the temperature after compression. Here  $C_P$  is the specific heat at constant pressure. [3 M]

(iii) The coefficient of compressibility ( $\beta$ ) of water at 298 K is 4.9 × 10<sup>-6</sup> atm<sup>-1</sup>, over the pressure range 1 to 25 atm. Calculate the amount of work required to compress a 1 mole liquid water from 1 atm. to 25 atm. at 298 K temperature. Compare this work with work involved in the compression of 1 mole ideal gas from 1 atm. to 25 atm. at 298 K temperature. In both cases consider the process as reversible. Please provide the unit in Joules. **(Density of water is 1 gm/ml at 298 K)** 

[**3 M**]

(iv) One mole of an ideal gas with  $C_V = 3.0$  cal  $K^{-1}$  mol<sup>-1</sup> initially at 273 K temperature, 1 atm. pressure and 22.4 litre volume is put through the following reversible cycle:

- (a) State 1 to state 2, heated at constant volume to twice the initial temperature.
- (b) State 2 to state 3 expanded adiabatically until it is back to initial temperature.

(c) State 3 to state 1 compressed isothermally back to state 1.

Depict the cycle in V vs T diagram and calculate the amount of heat transfer (q), work (w) and change in internal energy ( $\Delta U$ ) for this cycle. Write in just one sentence what conclusion you can derive from the results. [5 M]

**Q3.** (i) Calculate the enthalpy change ( $\Delta$ H) at 1500 K for the reaction  $2H_2(g) + O_2(g) \rightleftharpoons 2H_2O(g)$ , given that,  $\Delta$ H<sub>300K</sub> = 115.0 Kcal and the values of C<sub>P</sub> (cal mol<sup>-1</sup> K<sup>-1</sup>) are for H<sub>2</sub>(g) = 6.95 – 0.0002 T, O<sub>2</sub>(g) = 6.10 + 0.0032 T and H<sub>2</sub>O(g) = 7.19 + 0.0024 T. Here C<sub>P</sub> is the specific heat at constant pressure. [5 M]

(ii) Calculate the change in entropy,  $\Delta S$ , when 10 gm of ice at 0<sup>o</sup>C is added to 50 gm of water at 40<sup>o</sup>C in an isolated system. The latent heat of fusion of ice is 79.7 cal gm<sup>-1</sup>, the specific heat of water is 1 cal gm<sup>-1</sup> K<sup>-1</sup>. [4 M]

(iii) What is the boiling point of water at a place where the atmospheric pressure is 600 mm Hg? The latent heat of vaporization is 540 cal/gm. [3 M]

(iv) Calculate the change in Gibbs free energy ( $\Delta$ G) when 36 gm of water initially at 100<sup>o</sup>C and 10 atm. pressure are converted to vapor at 100<sup>o</sup>C and 0.01 atm. pressure. Given density of water is 1 gm/ml and the vapor obeys ideal gas law. [3 M]

**Q4**. (i) Calculate the number of phases (P), components (C) and degrees of freedom (F) of the following systems at equilibrium.

- (a) An aqueous solution of  $H_2SO_4$  and  $CH_3COOH$
- (b) Water at its freezing point.
- (c) A saturated solution of Na<sub>3</sub>PO<sub>4</sub> which is completely dissociates into its component ions, contains an excess of salt.

(ii) At 140<sup>o</sup>C, the vapor pressure of pure C<sub>6</sub>H<sub>5</sub>Cl is 939.4 mm of Hg and that of pure C<sub>6</sub>H<sub>5</sub>Br is 495.8 mm of Hg. If a liquid mixture of C<sub>6</sub>H<sub>5</sub>Cl and C<sub>6</sub>H<sub>5</sub>Br forms an ideal solution, what will be the composition of the mixture in the liquid phase, which boils at 140<sup>o</sup>C under 1 atm. pressure? What will be composition in the vapor phase at this temperature? [3 M]

(iii) The following standard enthalpies of formation ( $\Delta H_f^0$ ) and entropies ( $S^0$ ) of the substances at 25°C are given

Substance	$\Delta H_f^0(Kcal)$	$S^0$ (Cal $K^{-1}$ )
Methane (CH <sub>4</sub> , g)	-17.89	44.5
Formaldehyde (HCHO, g)	-27.7	52.3
Ethyl alcohol (C <sub>2</sub> H <sub>5</sub> OH, I)	-66.4	38.4

Calculate the standard free energy change and equilibrium constant at 25°C and 1 atm. pressure for the reaction  $CH_4(g) + HCHO(g) \rightleftharpoons C_2H_5OH(l)$ . [4 M]

(iv) Calculate activity coefficient of  $Ba^{2+}$  and  $Cl^-$  in a 0.05 M aqueous solution of  $BaCl_2$  at 25°C. Also determine the mean activity coefficient of  $BaCl_2$  in this solution at 25°C. The Debye-Huckel constant, A = 0.509 for an aqueous solution at 25°C. [3 M]