Birla Institute of Technology and Science, Pilani

First Semester 2017-18 Mid-Semester Examination (Part A Closed Book)

Course Title: Nanoelectronics & Nanophotonics Course No. EEE G595

Maximum Marks: 60 Maximum Time: 60 Minutes Dated: 9/10/2017

1.(a) From the expression for $h_0(\vec{k}) = -t(1 + 2e^{ik_x a} \cos k_y b)$ for a graphite sheet, use Taylor expansion about a Dirac point (k_xa, k_yb)=(0, $\pm 2\pi/3$) to obtain the energy dispersion relation for a CNT. Show that within this approximation, we obtain constant-energy contours of circles isotropically disposed around the center of Dirac point. [10]

(b) From the expression of the energy dispersion relation obtained in (a), calculate the minimum energy gap of a ZNT for sub-bands $v_1 = 60$ and $v_2 = 85$ whose circumferential vector is $\vec{c} = \hat{y}2bm$ where the value of m is 90. [10]

2. From the 3-D Schrödinger equation
$$\left[E_{C} - \frac{\hbar^{2}}{2m}\frac{\partial^{2}}{\partial x^{2}} - \frac{\hbar^{2}}{2m}\frac{\partial^{2}}{\partial y^{2}} - \frac{\hbar^{2}}{2m}\frac{\partial^{2}}{\partial z^{2}} + U(z)\right]\Phi_{\alpha}(\vec{r}) = E_{\alpha}\Phi_{\alpha}(\vec{r}) ,$$

obtain a 1-D Schrödinger equation for a z-strip, where electrons are free to move in \hat{x} and \hat{y} direction and there is a confinement along the \hat{z} direction. [10]

3. The Retarded Green's Function for the channel of a one-level device can be given as $G^{R}(E) = [E - \varepsilon' + i\gamma/2]^{-1}$. Now, from the expression of $G^{R}(E)$, obtain the expression for the density of states, D(E) in the channel and show that the broadened level in the channel of this one-level device can accommodate exactly the same number of electrons that a discrete level could accommodate before it got coupled to the reservoir. [20]

4. Calculate the Integral transforms:

(a)

$$I(t) = \int_{-\infty}^{\infty} \frac{dE}{2\pi\hbar} e^{-iEt/\hbar} \left(\frac{1}{E - \varepsilon_i + i0^+} \right)$$
[5]

(b)
$$I(E) = \int_{-\infty}^{\infty} I(t)e^{+iEt/\hbar}dt$$
 [5]

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Maximum Marks: 30 Maximum Time: 30 Minutes Dated: 9/10/2017

1. Obtain a 8×8 Tridiagonal Hamiltonian matrix for the following z-strip of AlGaAs/GaAs/AlGaAs by using one-band effective mass equation:



[15]

2. Obtain a Block-Tri-Diagonal Hamiltonian matrix for the channel a nano-scale 2D device which is rectangular lattice is shown is the figure.

