# Birla Institute of Technology \& Science, Pilani <br> Second Semester 2022-2023 <br> No. of Pages $=4$ <br> No. of Questions $=6$ 

## ME F318 Computer aided design - Comprehensive Exam

Weightage
Marks
: 40\% (As per Course Handout)
: 80
Duration $: 3.0$ Hours
NAME

Date of Exam : 13/05/2023 (FN)
ID No.
Note to Students:

1. All parts of a question should be answered only in the space provided below each question.
2. NO EXTRA SHEET WILL BE GIVEN. Give your answers to the point.
3. Assumptions made, if any, should be stated clearly at the beginning of your answer.
4. Verify Euler-Poincaré relation topological validity for B-rep models below. [12 Marks]


| $\mathrm{F}=\ldots$ |
| :--- |
| $\mathrm{E}=\ldots$ |
| $\mathrm{V}=\ldots$ |
| $\mathrm{L}=\ldots$ |
| $\mathrm{B}=\ldots$ |
| $\mathrm{G}=\ldots$ |



$$
\begin{aligned}
& \mathrm{F}=\ldots \\
& \mathrm{E}=\ldots \\
& \mathrm{V}=\ldots \\
& \mathrm{L}=\ldots \\
& \mathrm{B}=\ldots \\
& \mathrm{G}=\ldots
\end{aligned}
$$

2. Draw a neat sketch of a third order B-spline curve $P(u)$ and a second order B-spline curve $\mathrm{Q}(\mathrm{u})$. Control points for $\mathrm{P}(\mathrm{u})$ are $\left[\begin{array}{ll}0 & 0\end{array}\right]$, $\left[\begin{array}{ll}1 & 1\end{array}\right],\left[\begin{array}{ll}3 & 1\end{array}\right]$, and [40]. Control points for $\mathrm{Q}(\mathrm{u})$ are [04], [2 2], [2 0], and [0-2]. Find the intersection point between P and Q. [10 Marks]
3. A triangle, in a 2-D ( $x$ and $y$ ) space, with vertices [31], [5ll, and [42] is reflected about a line $y=x$. Obtain final transformation matrix and transformed vertices. [15 Marks]
4. Parametric equation of helix with radius a and pitch $b$ is $[\operatorname{acos} 2 \pi u$ asin $2 \pi u 2 b \pi u], 0 \leq u \leq 1$. Write its explicit equation and bring out the advantages of its parametric form. [8 Marks]
5. Derive $[B]$ of Hermite bicubic surface bounded by four lines shown in figure. [ $\mathbf{1 0}$ Marks]
6. Draw a neat sketch of a ruled surface $\mathrm{R}(\mathrm{u}, \mathrm{v})$ formed by the two linearly blending curves $P(u, 0)$ and $Q(u, 1) . P(u, 0)$ is a third order B-spline curve defined by control points [00], [11], [31], and [4 0 ]. $\mathrm{Q}(\mathrm{u}, 1)$ is also a third order B-spline curve defined by control points [05], [16], [3 6], and [4 5]. Compute the midpoint of the surface also.
[25 Marks]
