# BIRLA INSTITUTE OF TECHNOLOGY AND SCIENCE, PILANI COMPREHENSIVE EXAMINATION (Closed Book)

I Semester 2016-17

**DATE**: 14-12-2016

## **COMPUTATIONAL PHYSICS (PHY F313)**

Max Marks: 50

Max Time: 60 min

### 1. Solution of Laplace equation: [3x10]

- (a) Suggest a numerical method to find out the solution of Laplace equation,  $\nabla^2 V(\mathbf{r}) = 0$  in 2D.
- (b) How can you justify the basic assumptions of *Jacobi Relaxation* method that is sometimes used to find the potential at the required point.
- (c) Write down the psuedo code to execute the JR (or any other numerical method) method.

## 2. The charging of a capacitor in an RC circuit is represented by

$$R\frac{dq}{dt} = V - \frac{q}{C}$$
  $R = 100 \ \Omega, \ C = 150 \ \mu F, \ V = 12 \ V$ 

with q = 0, t = 0. Use Euler method to solve (in 5 steps) and find out the q(t = 0.005 s). Do you get the saturation in q(t)? Justify your answer. [20]

# BIRLA INSTITUTE OF TECHNOLOGY AND SCIENCE, PILANI COMPREHENSIVE EXAMINATION (Open Source)

I Semester 2016-17

**DATE**: 14-12-2016

Max Marks: 70

#### **COMPUTATIONAL PHYSICS (PHY F313)**

## IMPORTANT

- You have to solve these problems by the codes you have written for your assignments.
- The in-built functions of MATLAB etc. are not allowed to execute your codes.

### 1. Solving the differential equations: [30]

(a) The two coupled I order equations

$$\frac{dy}{dt} = p \qquad \qquad \frac{dp}{dt} = -4\pi^2 y$$

represent SHM with period 1. Using your RK-4 codes, solve these equations with any particular initial conditions and investigate the accuracy with which system returns to its initial state at integral values of t.

- (b) Solve the charging of capacitor problem (Q2 I part) by Improved Euler method. Plot the curve.
- 2. Consider a protein on a simple square lattice. The energy of model is defined as,

$$E = \sum_{\langle i,j \rangle} \delta_{ij} J_{A(i),A(j)}$$

where, the sum is over all pairs of proteins  $\langle i, j \rangle$  in the chain and  $\delta_{i,j} = 1$  if amino acids are nearest neighbour not connected by direct covelant bond. Consider 25 amino acids and assume that energy is measured in units of  $k_B$  and system is at temperature of 10. Using your Monte carlo codes (Metropolis based), simulate the different structures of protein. [40]