

Birla Institute of Technology and Science - Pilani, Pilani Campus

Semester I (Session 2022-23)

Midsemester Examination (Closed Book)

Particle Physics (PHYF 413)

Date : 01/11/2022

Weightage : 25 %

Time: 90 Mints.

Max. Marks: 25

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**Q1:** (a) Consider the following interaction process;  $A + B \rightarrow C + D + E$  with masses,  $m_A$ ,  $m_B$ ,  $m_C$  and  $m_D$  and  $m_E$ , respectively. Find the threshold kinetic energy of particle A in the lab frame to just produce the particles C, D and E. (b) Express 800 kg m/sec and 100 kg into energy units (Joule) and then convert it in MeV. [5]

**Q2:** Assuming collision process to be  $A + B + C \rightarrow 1 + 2 + 3$ ; Write an expression for  $dN$  (no. of available states for particles having momentum in the range  $\vec{p}$  to  $\vec{p} + \vec{d}\vec{p}$ ) using Dirac-delta function for momentum conservation. Also write relation between  $H_{fi}$  and Lorentz invariant matrix element  $M_{fi}$ . [5]

**Q3:** (a) Obtain Dirac equation in the covariant form. Also find square properties of Dirac gamma matrices using the properties of Dirac  $\alpha_s$  and  $\beta$  matrices. (b) Without solving Maxwell equation, I mean using an appropriate identity, determine the em potential  $A^\mu$  for a muons which constitute a four current given by  $J^\mu = -eN_A N_C (p_A + p_C)^\mu e^{i(p_C - p_A) \cdot x}$ , Here  $N_A$  and  $N_C$  are normalization constants. [5]

**Q4:** (a) Write Klein-Gordon equation for an alpha particle moving under the action of an em field given by  $A^\mu$ . (b) For scattering process  $A + B \rightarrow C + D$ , draw simplest t-channel Feynman diagram. Using Feynman rules for QED (forgetting the spin!), write an expression for Lorentz invariant amplitude  $-iM$ . [5]

**Q5:** For a two body decay process,  $A \rightarrow 1 + 2$ , write an expression for the decay rate using Fermi's golden rule in terms of 6D three momentum integral. Then integrate it to obtain the final expression for the Decay rate. [5]

\*\* Best Wishes \*\*